EFFECT OF MAGNETIC FIELD ON DOUBLE CONVECTION FLOW OF VISCOUS FLUID OVER A MOVING VERTICAL PLATE WITH CONSTANT TEMPERATURE AND GENERAL CONCENTRATION BY USING NEW TREND OF FRACTIONAL DERIVATIVE

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Abstract. This article presents, effects of fractional order derivative and magnetic field on double convection flow of viscous fluid over a moving vertical plate with constant temperature and general concentration. The model is fractionalized by using Caputo-Fabrizio derivative operator. Closed form solutions of the fluid velocity, concentration and temperature are obtained by means of the Laplace transform. Numerical computations and graphical illustrations are used in order to study the effects of the Caputo-Fabrizio time-fractional parameter, magnetic parameter, Prandtl and Grashof numbers on velocity field.

Mathematics Subject Classification: 05C69.

Key words and phrases: Free convection flow; MHD; Caputo-Fabrizio fractional derivative; Heat Absorption; Exact solutions.

1. Introduction

The enthusiasm in fluid mechanics is really meaningful in the presence of “transport phenomena, which is a significant feature in thermal, chemical, and mechanical engineering science. Several physical mechanism exists which can be used to transport thermal energy and chemical species through a phase and across boundaries of the phase. The three mechanisms for the heat transfer are diffusion, convection and radiation. Convection of heat transfer is further classified

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into three subsequent branches, namely; natural (free), forced, and mixed convection, depending upon the physical system initiating the motion of the fluid. Free convection flows resulting from the heat and mass transfer driven by the combined buoyancy effect due to temperature and concentration variations have been extensively studied, due to their various applications in geosciences, chemical engineering, and industrial activities as food processing and polymer production. Other multiple areas of applications such as: heat transfer from transmission lines and pipes, heat conduction from electrical devices, heat debauchery from the spiral refrigerator element to surrounding air, heat transfer from a heater, heat transfer in nuclear energy poles, extrusion and wiredrawing, atmospheric and oceanic circulation, etc., have been studied by Jaluria [1]. Free convection problems are usually formulated under different situations like constant surface temperature, ramped temperature at the wall or surface heat flux [2]. Generally, the mass transfer due to the concentration differences affects the rate of heat transfer. The driving force for the free convection is buoyancy so its effects cannot be neglected when the fluid velocity is small and temperature difference between the surface and ambient fluid is large enough [3-5]. Electrically conducting fluids also have received much attention from the researchers due to their large scale applications in industrial appliances. The magneto hydrodynamics (MHD) has its own practical applications, such as the cooling of nuclear reactors by liquid sodium and induction flow meter, which depends on the potential difference in the fluid in the direction perpendicular to the motion and to the magnetic field [6]. The influence of magnetic field on the free convection flow is significant in liquid metals, electrolytes and ionized gases. The work of Soundalgekar et al. [7] is seemed to be the first on mass transfer and magnetic effects. The study of MHD in the free convection has attracted the interest of many researchers in view of its applications in geophysics and astrophysics [8]. The role of "Fractional Calculus" which is now a day’s called calculus of 21th century in modern sciences and engineering is very significant. The tools devised in the subject is used in past few decades to provide solutions to hundreds of real world problems. Researchers are interested to solve scientific problems using the techniques developed in fractional calculus. In the recent times, fractional calculus has been extended to several directions for instance fractional-order multipoles in the electromagnetism, electrochemistry, models in mathematical biology, finance, fluid flows tracers, signal processing in engineering, applied mathematics, bio-engineering and fluid dynamics [9]. Many researchers in fluid dynamics widely used fractional derivative models to study the viscoelastic materials such as polymers in glass transition. It is vital to bring in light the fact that fractional derivative generalizations of one dimensional viscoelastic models have seen to be more useful in modeling the response linear regime [10]. This generalization is in good agreement with the second law of thermodynamics.
The fractional derivative operators used up till now, are Riemann-Liouville fractional derivative and Caputo fractional derivative operator \[11\]. It is observed by many researchers that application of these operators exhibit difficulties, such as Riemann-Liouville fractional derivative of constant functions is not zero, and its Laplace transform contain terms without physical significance. Caputo fractional derivative has eliminated these difficulties, but the kernel in its definition is a singular function. The results that are been found using these operators are expressed in complicated forms involving some generalized functions. Recently, Caputo and Fabrizio gave a new expression for fractional derivative operator with an exponential kernel without singularities. The Caputo-Fabrizio temporal-fractional derivative is suitable in the use of the Laplace transform. Shah et al. \[12\] applied the idea of the Caputo-Fabrizio fractional derivatives to generalize the starting flow of second grade fluid over a vertical plate and obtained the exact solutions using the Laplace transform technique. Some other recent studies can be found in \[13-17\] and the references therein.

2. Mathematical formulation of the problem

The unsteady magneto-hydrodynamic flow of viscous incompressible fluid past an infinite vertical plate and constant temperature and variable mass diffusion has been studied. Initially, the plate and the fluid are at the same temperature \(T_\infty\) in the stationary condition with concentration level \(C_\infty\) at all the points. At time \(t = 0^+\), the plate is moving with a velocity \(U_0 f(t)\) in its own plane and the temperature of the plate is constant \(T_w\) as well species concentration is raised or lowered to the value \(C_\infty + C_w g(t)\) with time. \(U_0\) is a constants with dimension of velocity while the dimensionless functions \(f(\cdot)\) and \(g(\cdot)\) are piecewise continuous of exponential order at infinity and \(f(0) = g(0) = 0\). We made the following assumptions:

- All fluid physical properties are considered to be constant except the influence of the body force terms.
- Applied magnetic field of uniform strength \(B_0\) is normal to the plate.
- The fluids conducting property is supposed to be slight and hence the magnetic Reynolds number is lesser than unity, the induced magnetic field is small in comparison with the transverse magnetic field.
- It is further supposed that there is no applied voltage, as the electric field is absent.
- Viscous dissipation and Joule heating in energy equation are neglected.

According to Boussinesq’s approximation, the unsteady flow is governed by the following set of equations:

\[
\frac{\partial u}{\partial t} = \nu \frac{\partial^2 u}{\partial y^2} + g\beta_T (T - T_\infty) + g\beta_C (C - C_\infty) - \frac{\sigma B_0^2}{\rho} u, \tag{1}
\]

\[
\rho c_p \frac{\partial T}{\partial t} = k \frac{\partial^2 T}{\partial y^2} - Q(T - T_\infty), \tag{2}
\]
\[
\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial y^2} - K_r (C - C_\infty),
\]
with initial and boundary conditions
\[
u = 0, T = T_\infty, C = C_\infty; t = 0, y > 0,
\]
\[
u = U_0 f(t), T = T_w, C(y, t) = C_\infty + (C_w - C_\infty) g(t); t > 0, y = 0,
\]
\[
u \rightarrow 0, T \rightarrow T_\infty, C \rightarrow C_\infty; y \rightarrow \infty, t > 0.
\]
Introducing the following dimensionless variables and parameters
\[
y^* = \frac{U_0 y}{\nu}, u^* = \frac{u}{U_0}, t^* = \frac{t U_0^2}{\nu}, T^* = \frac{T - T_\infty}{T_w - T_\infty}, C^* = \frac{C - C_\infty}{C_w - C_\infty},
\]
\[Gr = \frac{g_\beta \nu (T_w - T_\infty)}{U_0^3}, Gm = \frac{g_\beta \nu (C_w - C_\infty)}{U_0^3}, M = \frac{\sigma B_0^2 \nu}{\rho U_0^2},
\]
\[Pr = \frac{\nu \mu}{k}, Sc = \frac{\nu}{D}, S = \frac{Q \nu^2}{k U_0^3}, \lambda = \frac{K_r \nu^2}{D U_0^2},
\]
into Eqs. (1)-(6) and dropping the star notation, we have the following initial-boundary problem
\[
\frac{\partial u(y, t)}{\partial t} = \frac{\partial^2 u(y, t)}{\partial y^2} + Gr T(y, t) + Gm C(y, t) - M u(y, t),
\]
\[
\frac{\partial T(y, t)}{\partial t} = \frac{1}{Pr} \frac{\partial^2 T(y, t)}{\partial y^2} - \frac{S}{Pr} T(y, t),
\]
\[
\frac{\partial C(y, t)}{\partial t} = \frac{1}{Sc} \frac{\partial^2 C(y, t)}{\partial y^2} - \frac{\lambda}{Sc} C(y, t),
\]
with dimensionless initial and boundary conditions
\[
u(y, t) = 0, T(y, 0) = 0, C(y, 0) = 0; y > 0,
\]
\[
u(0, t) = f(t), T(0, t) = 1, C(0, t) = g(t); t > 0,
\]
\[
u(y, t) \rightarrow 0, T(y, t) \rightarrow 0, C(y, t) \rightarrow 0; y \rightarrow 0.
\]
Here, we have to developed fractional model, replacing the time derivative in Eqs. (8), (9) and (10), with time-fractional derivatives, we obtain the following fractional differential equations
\[
D_t^\alpha u(y, t) = \frac{\partial^2 u(y, t)}{\partial y^2} + Gr T(y, t) + Gm C(y, t) - M u(y, t),
\]
\[
D_t^\alpha T(y, t) = \frac{1}{Pr} \frac{\partial^2 T(y, t)}{\partial y^2} - \frac{S}{Pr} T(y, t),
\]
\[
D_t^\alpha C(y, t) = \frac{1}{Sc} \frac{\partial^2 C(y, t)}{\partial y^2} - \frac{\lambda}{Sc} C(y, t),
\]
where \(D_t^\alpha u(y, t)\) represent the Caputo-Fabrizio time-fractional derivative of \(u(y, t)\), defined as [17]
\[
D_t^\alpha u(y, t) = \frac{1}{1 - \alpha} \int_0^t u'(y, \tau) \exp \left( -\frac{\alpha (t - \tau)}{1 - \alpha} \right) d\tau, 0 < \alpha < 1.
\]
3. Solution of the problem

3.1. Calculation for temperature. Taking Laplace transform of Eqs. (15), (12)_2, (13)_2 and using initial condition Eq. (11)_2, we obtain

\[
\frac{\gamma q}{q + \alpha \gamma} \mathcal{T}(y, q) = \frac{1}{Pr} \frac{\partial^2 \mathcal{T}(y, q)}{\partial y^2} - \frac{S}{Pr \lambda} \mathcal{T}(y, q),
\]

(18)

\[
\mathcal{T}(0, q) = \frac{1}{q}, \mathcal{T}(y, q) \to 0 \text{ as } y \to \infty,
\]

(19)

where \( \gamma = \frac{1}{1 - \alpha} \), \( \mathcal{T}(y, q) \), is the Laplace transform of \( T(y, t) \) and \( q \) is the transform variable. The solution of the partial differential equation (18) by using conditions in equation (19), we obtain

\[
\mathcal{T}(y, q) = \frac{1}{q} \exp \left( -y \sqrt{\frac{Pr\gamma q}{q + \alpha \gamma} + S} \right)
\]

\[
= \frac{1}{q} \exp \left( -y \sqrt{\frac{(Pr\gamma + S)q + S\alpha \gamma}{q + \alpha \gamma}} \right)
\]

\[
= \frac{1}{q} \exp \left( -y \sqrt{\frac{(Pr\gamma + S)q + S}{\alpha \gamma q + 1}} \right)
\]

\[
= F_1\left( y, q, \frac{1}{\alpha \gamma}, S, \frac{Pr\gamma + S}{\alpha \gamma} \right),
\]

(20)

with inverse Laplace transform

\[
T(y, t) = f_1\left( y, t, \frac{1}{\alpha \gamma}, S, \frac{Pr\gamma + S}{\alpha \gamma} \right),
\]

(21)

where \( F_1(y, q, a, b, c) \) and \( f_1(y, t, a, b, c) \) are defined in Appendix.

3.2. Calculation for concentration. Taking Laplace transform of Eqs. (16), (12)_3, (13)_3 and using initial condition Eq. (11)_3, we obtain

\[
\frac{\gamma q}{q + \alpha \gamma} \mathcal{C}(y, q) = \frac{1}{Sc} \frac{\partial^2 \mathcal{C}(y, q)}{\partial y^2} - \frac{\lambda}{Sc} \mathcal{C}(y, q),
\]

(22)

\[
\mathcal{C}(0, q) = G(q), \mathcal{C}(y, q) \to 0 \text{ as } y \to \infty,
\]

(23)

where \( \frac{1}{\alpha \gamma} \mathcal{C}(y, q) \) and \( G(q) \) are the Laplace transform of \( C(y, t) \) respectively \( g(t) \) and \( q \) is the transform variable.

The solution of the partial differential equation (22) by using conditions in equation (23), we obtain

\[
\mathcal{C}(y, q) = G(q) \exp \left( -y \sqrt{\frac{Sc\gamma q}{q + \alpha \gamma} + \lambda} \right).
\]

(24)
Eq. (24) can be written in equivalent form as

\[
C(y; q) = q G(q) \int_{0}^{\infty} \frac{1}{q} \exp \left( -y \sqrt{\frac{(Sc\gamma + \lambda)q + \lambda}{\alpha\gamma q + 1}} \right) \]

\[
= q G(q) F_1 \left( y, q, \frac{1}{\alpha\gamma}, \lambda, \frac{Sc\gamma + \lambda}{\alpha\gamma} \right). \quad (25)
\]

Inverting Laplace transform we obtain the temperature distribution as

\[
C(y; t) = g'(t) * f_1 \left( y, t, \frac{1}{\alpha\gamma}, \lambda, \frac{Sc\gamma + \lambda}{\alpha\gamma} \right) \quad (26)
\]

where \( g'(t) = L^{-1} \{ qG(q) \} \), "*" represent the convolution product and \( F_1(y, q, a, b, c) \) are defined in Appendix.

### 3.3. Calculation for velocity.

Taking Laplace transform of Eqs. (14), (12)_1, (13)_1, using initial condition Eq. (11)_1, by introducing Eqs. (20) and (24), we obtain

\[
\left( \frac{\gamma q}{q + \alpha\gamma} + M \right) \tilde{\nu}(y, q) = \frac{\partial^2 \tilde{\nu}(y, q)}{\partial y^2} + Gr \frac{1}{q} \exp \left( -y \sqrt{\frac{Pr\gamma q}{q + \alpha\gamma} + S} \right)
\]

\[
+ Gm G(q) \exp \left( -y \sqrt{\frac{Pr\gamma q}{q + \alpha\gamma} + \lambda} \right), \quad (27)
\]

\[
\tilde{\nu}(0, q) = F(q), \tilde{\nu}(y, q) \to 0, \quad as \quad y \to \infty, \quad (28)
\]

where \( F(q) \) is the Laplace transform of \( f(t) \).

The solution of the partial differential equation (27) subject to conditions in equation (28) can be written in the following suitable form as

\[
\tilde{\nu}(y, q) = q F(q) F_1 \left( y, q, \frac{1}{\alpha\gamma}, M, \frac{\gamma + M}{\alpha\gamma} \right) + \tilde{\nu}_1(y, q) + \tilde{\nu}_2(y, q), \quad (29)
\]

where

\[
\tilde{\nu}_1(y, q) = \frac{Gra_3}{a_1} \left[ 1 + \frac{a_5}{q + a_4} \right] \left[ F_1 \left( y, q, \frac{1}{\alpha\gamma}, S, \frac{Pr\gamma + S}{\alpha\gamma} \right) - F_1 \left( y, q, \frac{1}{\alpha\gamma}, M, \frac{\gamma + M}{\alpha\gamma} \right) \right], \quad (30)
\]

\[
\tilde{\nu}_2(y, q) = \frac{Gma_3}{b_2} \cdot q G(q) \left[ 1 + \frac{b_4}{q + b_3} \right] \left[ F_1 \left( y, q, \frac{1}{\alpha\gamma}, \lambda, \frac{Sc\gamma + \lambda}{\alpha\gamma} \right) - F_1 \left( y, q, \frac{1}{\alpha\gamma}, M, \frac{\gamma + M}{\alpha\gamma} \right) \right], \quad (31)
\]
where \( a_1 = M - S, a_2 = a_3[(1 - Pr)\gamma + a_1], a_3 = \frac{1}{\alpha\gamma}, a_4 = \frac{a_2}{a_1}, a_5 = \frac{a_1 - a_2a_3}{a_1a_3}, \)

\( b_1 = M - \lambda, a_2 = a_3[(1 - Sc)\gamma + b_1], b_3 = \frac{b_1}{b_2}, b_4 = \frac{b_2 - a_3b_1}{a_3b_2} \)

and \( F_1(y, q, a, b, c) \) is defined in the Appendix.

Taking inverse Laplace transform of Eqs. (29), (30) and (31), we obtain

\[
\bar{u}(y,t) = f'(t) \ast f_1 \left( y, t, \frac{1}{\alpha\gamma}, M, \frac{\gamma + M}{\alpha\gamma} \right) + \bar{u}_1(y, t) + \bar{u}_2(y, t),
\]

where

\[
\begin{align*}
\overline{u}_1(y, t) &= \frac{Gr\alpha_3}{a_1} \left[ H(t) + a_5e^{-a_5t} \right] * \left[ f_1 \left( y, t, \frac{1}{\alpha\gamma}, S, \frac{Pr\gamma + S}{\alpha\gamma} \right) - F_1 \left( y, t, \frac{1}{\alpha\gamma}, M, \frac{\gamma + M}{\alpha\gamma} \right) \right], \\
\overline{u}_2(y, t) &= \frac{Gma_3}{b_2} g'(t) * [H(t) + b_4e^{-b_4t}] * \left[ f_1 \left( y, t, \frac{1}{\alpha\gamma}, \lambda, \frac{Sc\gamma + \lambda}{\alpha\gamma} \right) - f_1 \left( y, t, \frac{1}{\alpha\gamma}, M, \frac{\gamma + M}{\alpha\gamma} \right) \right],
\end{align*}
\]

and \( f_1(y, t, a, b, c) \), is defined in Appendix and “*” represent the convolution product.

### 4. Numerical results and discussions

In order to obtain some information on the fluid flow parameters, we have made several numerical simulations using Mathcad software. Obtained results are presented in the graphs from Figures 1-6. All the parameters and profiles are dimensionless.

We were interested to analyze the influence of the fractional parameter \( \alpha \) with different values of time \( t \), magnetic parameter \( M \), Prandtl number \( Pr \) and Grashof number \( Gr \) on velocity field in order to study the flow behavior.

In Fig. 1, we present the influence of the fractional parameter \( \alpha \) with small time \( t \) on velocity profile. It is observe that by increasing the value of the fractional parameter the velocity is decreases with small values of time and by increasing the time the velocity increase.

In Fig. 2, we present the influence of the fractional parameter \( \alpha \) with large time \( t \) on velocity profile. It is observe that by increasing the value of the fractional parameter the velocity is increases with large values of time and by increasing the time the velocity increase.

The effect of magnetic field for small and large values of time on velocity profile is presented in Fig. 3, respectively Fig. 4. It is observe that by increasing the magnetic field the velocity is decreases as which is expected for small as well as
for large time. The effect of Prandtl number $Pr$ and Grashof number $Gr$ are presented in Figs. 5 and 6, respectively. It is observe that the velocity decrease by increasing the Prandtl number $Pr$ and increase by increasing the values of $Gr$.

Fig. 1. Profile of dimensionless velocity versus $y$ for $\alpha$ variation with $Pr = 0.7, S = 5, Sc = 0.8, \lambda = 4, Gr = 3, Gm = 0.9, M = 0.4$ and different small values of time $t$.

Fig. 2. Profile of dimensionless velocity versus $y$ for $\alpha$ variation with $Pr = 0.7, S = 5, Sc = 0.8, \lambda = 4, Gr = 3, Gm = 0.9, M = 0.4$ and different large values of time $t$. 
Effect of magnetic field on double convection flow of viscous fluid

Fig. 3. Profile of dimensionless velocity versus $y$ for $\alpha$ variation with $Pr = 0.7, S = 5, Sc = 0.8, \lambda = 4, Gr = 3, Gm = 0.9$, and different values of $M$ for small time.

Fig. 4. Profile of dimensionless velocity versus $y$ for $\alpha$ variation with $Pr = 0.7, S = 5, Sc = 0.8, \lambda = 4, Gr = 3, Gm = 0.9$, and different values of $M$ for large time.
5. Conclusions

This aim of this article presents, the effects of fractional order derivative and magnetic field on double convection flow of viscous fluid over a moving vertical
plate with constant temperature and general concentration. Numerical computations and graphical illustrations are used in order to study the effects of the Caputo-Fabrizio time-fractional parameter $\alpha$, magnetic parameter $M$, Prandtl and Grashof number on velocity field. The follow important points are observed

- By increasing the value of the fractional parameter the velocity is decreases with small values of time and by increasing the time the velocity increase.
- By increasing the value of the fractional parameter the velocity is increases with large values of time and by increasing the time the velocity increase.
- By increasing the magnetic field the velocity is decreases.
- The velocity decrease by increasing the Prandtl number $Pr$.
- The velocity increase by increasing the values of $Gr$.

6. Appendix

\[
F_1(y, q, a, b, c) = \frac{1}{q} \exp \left( -y \sqrt{\frac{cq+b}{aq+1}} \right)
\]

\[
f_1(y, t; a, b, c) = L^{-1}\{F_1(y, q, a, b, c)\} = \begin{cases} 
\frac{c}{a} e^{-\frac{y^2}{2a}} \int_0^t \text{erfc} \left( \frac{y}{2\sqrt{u}} \right) e^{-\frac{aq}{u}} I_0 \left( \frac{2}{a} \sqrt{(c-ab)u} \right) du \\
b \int_0^\infty \int_0^t \text{erfc} \left( \frac{y}{2\sqrt{a}} \right) e^{-\frac{aq}{u}} I_0 \left( \frac{2}{a} \sqrt{(c-ab)u} \right) d\tau du, \quad 0 < \alpha < 1, \\
\psi(y, t, a, b), \quad \alpha = 1.
\end{cases}
\]

Competing Interests

The author(s) do not have any competing interests in the manuscript.

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Nomenclature

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tbody>
<tr>
<td>$B_0$</td>
<td>Uniform Applied Magnetic field,</td>
</tr>
<tr>
<td>$C_w$</td>
<td>Concentration on the plate,</td>
</tr>
<tr>
<td>$C_\infty$</td>
<td>Concentration of the fluid far away from the plate,</td>
</tr>
<tr>
<td>$c_p$</td>
<td>Specific heat at constant pressure,</td>
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<tr>
<td>$D$</td>
<td>Solute mass diffusivity</td>
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<td>$g$</td>
<td>Acceleration due to gravity,</td>
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<td>$Gr$</td>
<td>Grashof number for heat transfer</td>
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<tr>
<td>$Gm$</td>
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<td>$K_r$</td>
<td>Dimensional Chemical reaction parameter</td>
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<td>Magnetic field parameter</td>
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<td>$T_w$</td>
<td>Temperature of the plate,</td>
</tr>
<tr>
<td>$T_\infty$</td>
<td>Temperature of the fluid far away from the plate</td>
</tr>
<tr>
<td>$\beta_T$</td>
<td>Thermal expansion coefficient,</td>
</tr>
<tr>
<td>$\beta_C$</td>
<td>Volumetric coefficient of expansion with species concentration,</td>
</tr>
<tr>
<td>$\nu$</td>
<td>Kinematic viscosity,</td>
</tr>
<tr>
<td>$\rho$</td>
<td>Density of the fluid,</td>
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<tr>
<td>$\sigma$</td>
<td>Electric conductivity</td>
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